



National
Qualifications
2018

2018 Mathematics

National 5 - Paper 2

Finalised Marking Instructions

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General marking principles for National 5 Mathematics

Always apply these general principles. Use them in conjunction with the detailed marking instructions, which identify the key features required in candidates' responses.

For each question, the marking instructions are generally in two sections:

- *generic scheme – this indicates why each mark is awarded*
- *illustrative scheme – this covers methods which are commonly seen throughout the marking*

In general, you should use the illustrative scheme. Only use the generic scheme where a candidate has used a method not covered in the illustrative scheme.

- (a) Always use positive marking. This means candidates accumulate marks for the demonstration of relevant skills, knowledge and understanding; marks are not deducted for errors or omissions.
- (b) If you are uncertain how to assess a specific candidate response because it is not covered by the general marking principles or the detailed marking instructions, you must seek guidance from your team leader.
- (c) One mark is available for each •. There are no half marks.
- (d) If a candidate's response contains an error, all working subsequent to this error must still be marked. Only award marks if the level of difficulty in their working is similar to the level of difficulty in the illustrative scheme.
- (e) Only award full marks where the solution contains appropriate working. A correct answer with no working receives no mark, unless specifically mentioned in the marking instructions.
- (f) Candidates may use any mathematically correct method to answer questions, except in cases where a particular method is specified or excluded.
- (g) If an error is trivial, casual or insignificant, for example $6 \times 6 = 12$, candidates lose the opportunity to gain a mark, except for instances such as the second example in point (h) below.

- (h) If a candidate makes a transcription error (question paper to script or within script), they lose the opportunity to gain the next process mark, for example

This is a transcription error and so the mark is not awarded.

$$x^2 + 5x + 7 = 9x + 4$$

This is no longer a solution of a quadratic equation, so the mark is not awarded.

$$x - 4x + 3 = 0$$

$$x = 1$$

The following example is an exception to the above

This error is not treated as a transcription error, as the candidate deals with the intended quadratic equation. The candidate has been given the benefit of the doubt and all marks awarded.

$$x^2 + 5x + 7 = 9x + 4$$

$$x - 4x + 3 = 0$$

$$(x - 3)(x - 1) = 0$$

$$x = 1 \text{ or } 3$$

(i) **Horizontal/vertical marking**

If a question results in two pairs of solutions, apply the following technique, but only if indicated in the detailed marking instructions for the question.

Example:

$$\begin{array}{cc} \bullet^5 & \bullet^6 \\ \bullet^5 & x = 2 \quad x = -4 \\ \bullet^6 & y = 5 \quad y = -7 \end{array}$$

Horizontal: $\bullet^5 x = 2 \text{ and } x = -4$ Vertical: $\bullet^5 x = 2 \text{ and } y = 5$
 $\bullet^6 y = 5 \text{ and } y = -7$ $\bullet^6 x = -4 \text{ and } y = -7$

You must choose whichever method benefits the candidate, **not** a combination of both.

- (j) In final answers, candidates should simplify numerical values as far as possible unless specifically mentioned in the detailed marking instruction. For example

$$\frac{15}{12} \text{ must be simplified to } \frac{5}{4} \text{ or } 1\frac{1}{4} \quad \frac{43}{1} \text{ must be simplified to } 43$$

$$\frac{15}{0.3} \text{ must be simplified to } 50 \quad \frac{4/5}{3} \text{ must be simplified to } \frac{4}{15}$$

$$\sqrt{64} \text{ must be simplified to } 8^*$$

*The square root of perfect squares up to and including 100 must be known.

- (k) Commonly Observed Responses (COR) are shown in the marking instructions to help mark common and/or non-routine solutions. CORs may also be used as a guide when marking similar non-routine candidate responses.
- (l) Do not penalise candidates for any of the following, unless specifically mentioned in the detailed marking instructions:

- working subsequent to a correct answer
- correct working in the wrong part of a question
- legitimate variations in numerical answers/algebraic expressions, for example angles in degrees rounded to nearest degree
- omission of units
- bad form (bad form only becomes bad form if subsequent working is correct), for example

$(x^3 + 2x^2 + 3x + 2)(2x + 1)$ written as

$(x^3 + 2x^2 + 3x + 2) \times 2x + 1$

$= 2x^4 + 5x^3 + 8x^2 + 7x + 2$

gains full credit

- repeated error within a question, but not between questions or papers
- (m) In any ‘Show that...’ question, where candidates have to arrive at a required result, the last mark is not awarded as a follow-through from a previous error, unless specified in the detailed marking instructions.
- (n) You must check all working carefully, even where a fundamental misunderstanding is apparent early in a candidate’s response. You may still be able to award marks later in the question so you must refer continually to the marking instructions. The appearance of the correct answer does not necessarily indicate that you can award all the available marks to a candidate.
- (o) You should mark legible scored-out working that has not been replaced. However, if the scored-out working has been replaced, you must only mark the replacement working.
- (p) If candidates make multiple attempts using the same strategy and do not identify their final answer, mark all attempts and award the lowest mark. If candidates try different valid strategies, apply the above rule to attempts within each strategy and then award the highest mark.

For example:

Strategy 1 attempt 1 is worth 3 marks.	Strategy 2 attempt 1 is worth 1 mark.
Strategy 1 attempt 2 is worth 4 marks.	Strategy 2 attempt 2 is worth 5 marks.
From the attempts using strategy 1, the resultant mark would be 3.	From the attempts using strategy 2, the resultant mark would be 1.

In this case, award 3 marks.

Detailed marking instructions for each question

Question		Generic scheme	Illustrative scheme	Max mark										
1.		<ul style="list-style-type: none"> •¹ know how to decrease by 2% •² know how to calculate new total •³ carry out calculations correctly within a valid strategy 	<ul style="list-style-type: none"> •¹ $\times 0.98$ •² $125\,000 \times 0.98^3$ •³ 117 649 (tonnes) 	3										
<p>Notes:</p> <ol style="list-style-type: none"> 1. Correct answer without working award 3/3 2. Where an incorrect percentage is used, the working must be followed through to give the possibility of awarding 2/3, with working eg $125\,000 \times 0.02^3 = 1$, with working award 2/3 $\times\check{\check{\check{}}}$ 3. Where division is used <ol style="list-style-type: none"> (a) along with 0.98, •¹ is not available eg $125\,000 \div 0.98^3 = 132810(.3\dots)$ award 2/3 $\times\check{\check{\check{}}}$ (b) along with an incorrect percentage, •¹ and •² are not available eg $125\,000 \div 1.02^3 = 117790(.2\dots)$ award 1/3 $\times\times\check{\check{}}$ 														
<p>Commonly Observed Responses: Working must be shown:</p> <table style="width: 100%; border-collapse: collapse;"> <tbody> <tr> <td style="width: 60%;">1. $125\,000 \times 1.02^3 = 132651$</td> <td style="text-align: right;">award 2/3 $\times\check{\check{\check{}}}$</td> </tr> <tr> <td>2. $125\,000 \times 0.98 = 122500$</td> <td style="text-align: right;">award 1/3 $\check{\times}\times$</td> </tr> <tr> <td>3. $125\,000 \times 0.98 \times 3 = 367500$</td> <td style="text-align: right;">award 1/3 $\check{\times}\times$</td> </tr> <tr> <td>4. $125\,000 \times 0.02 = 2500 \rightarrow 125000 - 3 \times 2500 = 117500$</td> <td style="text-align: right;">award 1/3 $\check{\times}\times$</td> </tr> <tr> <td>5. $125\,000 \times 0.02 \times 3 = 7500$</td> <td style="text-align: right;">award 0/3</td> </tr> </tbody> </table>					1. $125\,000 \times 1.02^3 = 132651$	award 2/3 $\times\check{\check{\check{}}}$	2. $125\,000 \times 0.98 = 122500$	award 1/3 $\check{\times}\times$	3. $125\,000 \times 0.98 \times 3 = 367500$	award 1/3 $\check{\times}\times$	4. $125\,000 \times 0.02 = 2500 \rightarrow 125000 - 3 \times 2500 = 117500$	award 1/3 $\check{\times}\times$	5. $125\,000 \times 0.02 \times 3 = 7500$	award 0/3
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5. $125\,000 \times 0.02 \times 3 = 7500$	award 0/3													

Question		Generic scheme	Illustrative scheme	Max mark
2.		<p>Method 1</p> <ul style="list-style-type: none"> •¹ appropriate fraction •² correct substitution into arc length formula •³ calculate arc length <p>Method 2</p> <ul style="list-style-type: none"> •¹ appropriate fraction •² correct substitution into arc length formula •³ calculate arc length 	<p>Method 1</p> <ul style="list-style-type: none"> •¹ $\frac{320}{360}$ •² $\frac{320}{360} \times 2 \times \pi \times 7 \cdot 4$ •³ 41(.32...) (cm) <p>Method 2</p> <ul style="list-style-type: none"> •¹ $\frac{360}{320}$ •² $2 \times \pi \times 7 \cdot 4 \div \frac{360}{320}$ •³ 41(.32...) (cm) 	3

Question	Generic scheme	Illustrative scheme	Max mark
<p>Notes:</p> <ol style="list-style-type: none"> Correct answer without working award 0/3 Do not penalise variations in π eg $\frac{320}{360} \times 2 \times 3.14 \times 7.4 = 41(.30\dots)$ award 3/3 Premature rounding: rounded working must be to at least 2 significant figures eg (a) $\frac{320}{360} \times 2 \times \pi \times 7.4 = 0.89 \times 2 \times \pi \times 7.4 = 41(.38\dots)$ award 3/3 (b) $\frac{320}{360} \times 2 \times \pi \times 7.4 = 0.9 \times 2 \times \pi \times 7.4 = 42$ or $41.8(46\dots)$ award 2/3 ✓✓x Accept $2 \times \pi \times 7.4 - \frac{40}{360} \times 2 \times \pi \times 7.4 = 41$ or $41(.32\dots)$ award 3/3 For subsequent incorrect working, the final mark is not available eg $2 \times \pi \times 7.4 - \frac{320}{360} \times 2 \times \pi \times 7.4 = 5$ or $5(.16\dots)$ award 2/3 ✓✓x 			
<p>Commonly Observed Responses: Working must be shown:</p> <ol style="list-style-type: none"> $\frac{320}{360} \times \pi \times 7.4 = 21$ or $20.6(64\dots)$ award 2/3 ✓x✓ $\frac{320}{360} \times \pi \times 7.4^2 = 153$ or $152.9(18\dots)$ award 2/3 ✓x✓ $\frac{40}{360} \times 2 \times \pi \times 7.4 = 5(.16\dots)$ award 2/3 x✓✓ $\frac{40}{360} \times \pi \times 7.4 = 3$ or 2.6 or $2.5(83\dots)$ award 1/3 xx✓ $\frac{40}{360} \times \pi \times 7.4^2 = 19(.11\dots)$ award 1/3 xx✓ $2 \times \pi \times 7.4 = 46(.49\dots)$ award 0/3 			

Question		Generic scheme	Illustrative scheme	Max mark
3.		<ul style="list-style-type: none"> •¹ start process •² solution 	<ul style="list-style-type: none"> •¹ $24^2 + (-12)^2 + 8^2$ •² 28 	2
<p>Notes:</p> <ol style="list-style-type: none"> 1. Correct answer without working award 2/2 2. Accept $24^2 + 12^2 + 8^2$ for the award of •¹ 3. For eg $\sqrt{24^2 + (-12)^2} = \sqrt{720} = 26 \cdot 8(3\dots)$ or $12\sqrt{5}$ award 0/2 				
<p>Commonly Observed Responses: No working necessary:</p> <ol style="list-style-type: none"> 1. $\sqrt{784}$ or 784 award 1/2 ✓ x 2. $22 \cdot 2(7\dots)$ or $4\sqrt{31}$ ($\sqrt{24^2 - 12^2 + 8^2} = \sqrt{496}$) award 1/2 x✓ 3. $\sqrt{496}$ award 0/2 4. $\sqrt{20} = 4 \cdot 4\dots$ ($\sqrt{24 - 12 + 8}$) award 0/2 				

Question		Generic scheme	Illustrative scheme	Max mark
4.		<ul style="list-style-type: none"> •¹ start to process right hand side •² collect like terms •³ solve for x 	<ul style="list-style-type: none"> •¹ $6x - 6 - 12$ •² $-3x < -18$ or $18 < 3x$ •³ $x > 6$ or $6 < x$ 	3
<p>Notes:</p> <ol style="list-style-type: none"> 1. Correct answer without valid working award 0/3 Treat guess and check as invalid working 2. For subsequent incorrect working final mark is not available eg $6 < x \rightarrow x < 6$ award 2/3 				
<p>Commonly Observed Responses:</p> <ol style="list-style-type: none"> 1. $3x < 6x - 6 - 12 \rightarrow 3x < -18 \rightarrow x < -6$ award 1/3 ✓×× 2. $3x < 6x - 1 - 12 \rightarrow -3x < -13 \rightarrow x > \frac{13}{3}$ award 2/3 ×✓✓ 3. (a) $3x = 6x - 6 - 12 \rightarrow -3x = -18 \rightarrow x = 6 \rightarrow x > 6$ award 3/3 (b) $3x = 6x - 6 - 12 \rightarrow -3x = -18 \rightarrow x = 6$ award 2/3 ✓✓× 				

Question		Generic scheme	Illustrative scheme	Max mark
5.	(a)	<p>Method 1</p> <ul style="list-style-type: none"> •¹ calculate mean •² calculate $(x - \bar{x})^2$ •³ substitute into formula •⁴ calculate standard deviation <p>Method 2</p> <ul style="list-style-type: none"> •¹ calculate mean •² calculate $\sum x$ and $\sum x^2$ •³ substitute into formula •⁴ calculate standard deviation 	<p>Method 1</p> <ul style="list-style-type: none"> •¹ 126 •² 36, 0, 1, 25, 16, 4 •³ $\sqrt{\frac{82}{5}}$ •⁴ 4(·049...) <p>Method 2</p> <ul style="list-style-type: none"> •¹ 126 •² 756, 95338 •³ $\sqrt{\frac{95338 - \frac{756^2}{6}}{5}}$ •⁴ 4(·049...) 	4
<p>Notes:</p> <ol style="list-style-type: none"> 1. For 126 and 4(·04...) without working award 1/4 ✓ x x x 2. Accept (standard deviation =) 4·04 with working 3. (a) For 126 and $\frac{\sqrt{82}}{5} = 4(·049...)$ award 4/4 (b) For 126 and $\frac{\sqrt{82}}{5} = 1(·811...)$ award 3/4 ✓ ✓ x ✓ 				
<p>Commonly Observed Responses:</p>				

Question		Generic scheme	Illustrative scheme	Max mark
5.	(b)	<ul style="list-style-type: none"> •¹ compare means •² compare standard deviations 	<ul style="list-style-type: none"> •¹ eg on average the number of customers was higher on Saturday •² eg the number of customers was less varied on Saturday 	2

Notes:

1. Answers must be consistent with answers to part (a)
2. Statements must involve
 - (a) reference to number of customers **and** a chronological comparison or reference to Saturday and/or Sunday
 - Accept eg ‘there were more customers on Saturday’
‘on average the number of customers decreased’
 - Do **not** accept eg ‘there were more visits on Saturday’,
‘the customers were more consistent on Saturday’
‘on average the number of customers was more’
3. For the award of •¹
 - (a) eg Accept
 - Saturday’s average number of customers was more
 - The amount of people was higher on Saturday
 - (b) eg Do **not** accept
 - The mean number of customers on Saturday was more
 - There were more customers at each stall on Saturday
 - The average number of people visiting the stalls was better
4. For the award of •²
 - (a) eg Accept
 - The spread of customer numbers on Saturday was less
 - The number of customers on Saturday was more consistent
 - Saturday’s customer numbers were less varied
 - (b) eg Do **not** accept
 - The standard deviation on Saturday was less
 - The range of customer numbers on Saturday was less
 - The customers on Saturday were less varied
 - On average the number of customers on Saturday was less varied
 - The standard deviation is more consistent

Commonly Observed Responses:

Question		Generic scheme	Illustrative scheme	Max mark
6.		<ul style="list-style-type: none"> •¹ valid strategy •² state value of a 	<ul style="list-style-type: none"> •¹ $5+4a=73$ or $5+4\times 17$ •² ($a=$)17 	2
<p>Notes:</p> <ol style="list-style-type: none"> 1. Correct answer without working award 2/2 2. Accept $f(17)=73$ without working award 2/2 3. Accept use of x in place of a 				
<p>Commonly Observed Responses:</p> <ol style="list-style-type: none"> 1. $5+4\times 73=297$ award 0/2 2. $5+4a=73$ or $5+4\times 17\rightarrow a=17\rightarrow f(a)=17$ award 2/2 3. $5+4a=73$ or $5+4\times 17\rightarrow f(a)=17$ award 1/2 ✓x 4. $f(73)=5+4x\rightarrow x=17$ award 2/2 				

Question		Generic scheme	Illustrative scheme	Max mark
7.		<ul style="list-style-type: none"> •¹ substitute into formula •² calculate volume •³ round to 2 significant figures 	<ul style="list-style-type: none"> •¹ $\frac{4}{3} \times \pi \times 3 \cdot 2^3$ •² $137 \cdot 2 \dots$ •³ $140(\text{cm}^3)$ 	3

Notes:

1. Correct answer without working award 0/3

2. Accept variations in π

eg $\frac{4}{3} \times 3 \cdot 14 \times 3 \cdot 2^3 = 137 \cdot 188 \dots = 140$

Commonly Observed Responses:

1. $\frac{4}{3} \times \pi \times 6 \cdot 4^3 = 1098 \cdot 0 \dots = 1100$ award 2/3 x✓✓

2. $\frac{4}{3} \times \pi \times 3 \cdot 2^2 = 42 \cdot 8 \dots = 43$ award 2/3 x✓✓

3. $\frac{4}{3} \times \pi \times 3 \cdot 2^3 = 42 \cdot 8 \dots = 43$ award 2/3 ✓x✓

4. $\frac{4}{3} \times \pi \times 3 \cdot 2 = 13 \cdot 4 \dots = 13$ award 1/3 xx✓

Question		Generic scheme	Illustrative scheme	Max mark
8.		<ul style="list-style-type: none"> •¹ rearrange equation •² calculate value of x •³ calculate 2nd value of x 	<ul style="list-style-type: none"> •¹ $\sin x = \frac{1}{7}$ •² $8 \cdot 2(1 \dots)$ •³ $171 \cdot 8$ or $171 \cdot 7(8 \dots)$ 	3

Notes:

1. Correct answers without working award 1/3 $\times \times \checkmark$
2. Accept 8 and 172 with valid working
3. Degree signs are not required
4. Premature rounding: rounded working must be to at least 2 decimal places
eg (a) $\sin x = \frac{1}{7} = 0 \cdot 14 \rightarrow x = 8 \cdot (04 \dots), 172$ or $171 \cdot (95 \dots)$ award 3/3
(b) $\sin x = \frac{1}{7} = 0 \cdot 1 \rightarrow x = 6$ or $5 \cdot (73 \dots), 174 \cdot (26 \dots)$ award 2/3 $\checkmark \times \checkmark$
5. Inappropriate use of RAD or GRAD should only be penalised once in Q8, Q9, Q13 or Q17
(a) $0 \cdot 143 \dots, 179 \cdot 856 \dots$ (RAD)
(b) $9 \cdot 125 \dots, 170 \cdot 874 \dots$ (GRAD)

Commonly Observed Responses:

1. $\sin x = \frac{5}{7} \rightarrow x = 45 \cdot 6, 134 \cdot 4$ award 2/3 $\times \checkmark \checkmark$
2. (a) $\sin x = -\frac{1}{7} \rightarrow x = 188 \cdot 2, 351 \cdot 8$ award 2/3 $\times \checkmark \checkmark$
(b) $\sin x = -\frac{1}{7} \rightarrow x = 8 \cdot 2, 171 \cdot 8$ award 0/3

Question		Generic scheme	Illustrative scheme	Max mark
9.		<ul style="list-style-type: none"> •¹ correct substitution into sine rule •² re-arrange formula •³ calculate length 	<ul style="list-style-type: none"> •¹ $\frac{20}{\sin 37} = \frac{DC}{\sin 105}$ •² $\frac{20 \sin 105}{\sin 37}$ •³ 32(.1... cm) 	3

Notes:

1. Correct answer without working award 0/3
2. Degree signs are not required
3. **BEWARE** $\frac{20}{\sin 37} = \frac{DC}{\sin 75} \rightarrow 32(.1\dots)$ award 2/3 x✓✓
4. Disregard errors due to premature rounding provided there is evidence
5. Inappropriate use of RAD or GRAD should only be penalised once in Q8, Q9, Q13 or Q17
 - (a) 30(.16...) (RAD)
 - (b) 36(.31...) (GRAD)

Commonly Observed Responses:

1. $\frac{20}{\sin 37} = \frac{?}{\sin 38} \rightarrow \frac{20 \sin 38}{\sin 37} = 20(.46\dots)$ award 2/3 x✓✓
2. $\frac{20}{37} = \frac{DC}{105} \rightarrow 57$ or $56(.7\dots)$ award 0/3

Question	Generic scheme	Illustrative scheme	Max mark
10.	<ul style="list-style-type: none"> •¹ express \overrightarrow{ED} in terms of \mathbf{u} and \overrightarrow{DC} in terms of \mathbf{w} •² express \overrightarrow{BC} in terms of \mathbf{u} and \mathbf{w} in simplest form 	<ul style="list-style-type: none"> •¹ $\overrightarrow{ED} = 2\mathbf{u}$ and $\overrightarrow{DC} = \frac{1}{2}\mathbf{w}$ •² $\mathbf{u} - \frac{1}{2}\mathbf{w}$ 	2

Notes:

1. Correct answer without working award 2/2
2. Accept $\mathbf{u} + -\frac{1}{2}\mathbf{w}$ award 2/2
3. Evidence for the award of •¹ may appear on the diagram
4. For the award of •¹ accept
 - (a) $-\mathbf{u} - \mathbf{w} + 2\mathbf{u} + \frac{1}{2}\mathbf{w}$
 - (b) $-\mathbf{u} - \mathbf{w} + 2\overrightarrow{AB} + \frac{1}{2}\overrightarrow{EA}$
5. $\overrightarrow{BA} + \overrightarrow{AE} + \overrightarrow{ED} + \overrightarrow{DC}$ alone is not enough for the award of •¹
6. For $-\mathbf{u} + \frac{1}{2}\mathbf{w}$
 - (a) without working award 0/2
 - (b) but may be worth 1/2 if there is valid working

Commonly Observed Responses:

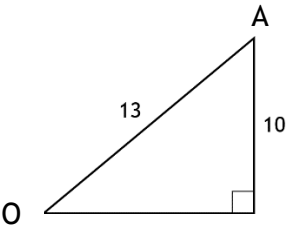
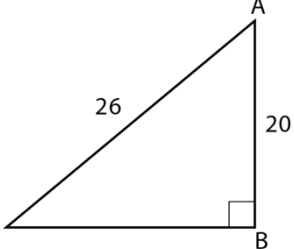
Question		Generic scheme	Illustrative scheme	Max mark
11.		<ul style="list-style-type: none"> •¹ know that $85\% = 9.3 \times 10^{11}$ •² begin valid strategy •³ complete calculation within valid strategy 	<ul style="list-style-type: none"> •¹ $85\% = 9.3 \times 10^{11}$ •² $1\% = \frac{9.3 \times 10^{11}}{85}$ •³ $1.094... \times 10^{12}$ (km³) or 1094117647000 (km³) 	3

Notes:

1. 1.1×10^{12}
(a) with valid working award 3/3
(b) without working award 0/3
2. **BEWARE**
 115% of $9.3 \times 10^{11} = 1.1 \times 10^{12}$ or $1.06... \times 10^{12}$
(a) and evidence of •¹ award 1/3 ✓xx
(b) otherwise award 0/3
3. 85% of $9.3 \times 10^{11} = 7.9(05) \times 10^{11}$
(a) and evidence of •¹ award 1/3 ✓xx
(b) otherwise award 0/3
4. Do not accept eg $10.94... \times 10^{11}$ for the award of •³

Commonly Observed Responses:

1. $\frac{9.3 \times 10^{11}}{0.85} = 1.094... \times 10^{12}$ award 3/3
2. $115\% = 9.3 \times 10^{11} \rightarrow \frac{9.3 \times 10^{11}}{1.15} = 8.086... \times 10^{11}$ award 2/3 x✓✓
3. $15\% = 9.3 \times 10^{11} \rightarrow \frac{9.3 \times 10^{11}}{0.15} = 6.2 \times 10^{12}$ award 2/3 x✓✓

Question	Generic scheme	Illustrative scheme	Max mark
12.	<p>Method 1</p> <ul style="list-style-type: none"> •¹ marshal facts and recognise right angled triangle •² consistent Pythagoras statement •³ calculate x •⁴ calculate width <p>Method 2</p> <ul style="list-style-type: none"> •¹ marshal facts and recognise right angled triangle •² consistent Pythagoras statement •³ calculate x •⁴ calculate width 	<ul style="list-style-type: none"> •¹  •² $x^2 = 13^2 - 10^2$ •³ $8.3(\dots)$ •⁴ $21.3(\dots \text{ cm})$ <ul style="list-style-type: none"> •¹  •² $x^2 = 26^2 - 20^2$ •³ $16.6(\dots)$ •⁴ $21.3(\dots \text{ cm})$ 	4

Question	Generic scheme	Illustrative scheme	Max mark																								
<p>Notes:</p> <ol style="list-style-type: none"> Correct answer without working award 0/4 In the absence of a diagram accept $x^2 = 13^2 - 10^2$ or $x^2 = 26^2 - 20^2$ as evidence for the award of •¹ and •² BEWARE Where a diagram is shown, working must be consistent with the diagram •² is not available for an <u>incorrect</u> diagram leading to $x^2 = 13^2 - 10^2$ or $x^2 = 26^2 - 20^2$ •² is available for a valid trig. method Where a candidate assumes the sizes of one or both of the smaller angles in the right-angled triangle, only •¹ and •⁴ are available •⁴ is only available following a Pythagoras (or trig.) calculation within a right-angled triangle involving 13 and 10 or 26 and 20 Disregard errors due to premature rounding provided there is evidence 																											
<p>Commonly Observed Responses:</p> <ol style="list-style-type: none"> $x^2 = 13^2 + 10^2 \rightarrow x = 16.4$; width = 29.4 <table data-bbox="220 1084 1203 1223"> <tr> <td>(a) working inconsistent with correct diagram</td> <td>award 3/4</td> <td>✓x✓✓</td> </tr> <tr> <td>(b) working consistent with candidate's diagram (cosine rule may be used to calculate x)</td> <td>award 3/4</td> <td>x✓✓✓</td> </tr> <tr> <td>(c) no diagram</td> <td>award 2/4</td> <td>xx✓✓</td> </tr> </table> $x^2 = 26^2 + 20^2 \rightarrow x = 32.8$; width = 29.4 <table data-bbox="220 1308 1203 1447"> <tr> <td>(a) working inconsistent with correct diagram</td> <td>award 3/4</td> <td>✓x✓✓</td> </tr> <tr> <td>(b) working consistent with candidate's diagram (cosine rule may be used to calculate x)</td> <td>award 3/4</td> <td>x✓✓✓</td> </tr> <tr> <td>(c) no diagram</td> <td>award 2/4</td> <td>xx✓✓</td> </tr> </table> $x^2 = 20^2 - 13^2 \rightarrow x = 15.2$; width = 28.2 <table data-bbox="220 1532 1203 1630"> <tr> <td>(a) working consistent with candidate's diagram (cosine rule may be used to calculate x)</td> <td>award 2/4</td> <td>x✓✓x</td> </tr> <tr> <td>(b) no diagram</td> <td>award 1/4</td> <td>xx✓x</td> </tr> </table> 				(a) working inconsistent with correct diagram	award 3/4	✓x✓✓	(b) working consistent with candidate's diagram (cosine rule may be used to calculate x)	award 3/4	x✓✓✓	(c) no diagram	award 2/4	xx✓✓	(a) working inconsistent with correct diagram	award 3/4	✓x✓✓	(b) working consistent with candidate's diagram (cosine rule may be used to calculate x)	award 3/4	x✓✓✓	(c) no diagram	award 2/4	xx✓✓	(a) working consistent with candidate's diagram (cosine rule may be used to calculate x)	award 2/4	x✓✓x	(b) no diagram	award 1/4	xx✓x
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(b) no diagram	award 1/4	xx✓x																									

Question		Generic scheme	Illustrative scheme	Max mark
13.		<ul style="list-style-type: none"> •¹ correct substitution into cosine rule •² correct calculation of $\cos YTF$ •³ calculate angle YTF •⁴ calculate bearing 	<ul style="list-style-type: none"> •¹ $\frac{10 \cdot 3^2 + 5 \cdot 6^2 - 7 \cdot 2^2}{2 \times 10 \cdot 3 \times 5 \cdot 6}$ •² $\frac{85 \cdot 61}{115 \cdot 36} (= 0 \cdot 742 \dots)$ •³ $42(-088 \dots)$ •⁴ $282(-088 \dots)$ 	4

Question	Generic scheme	Illustrative scheme	Max mark
<p>Notes:</p> <ol style="list-style-type: none"> Correct answer without working award 0/4 For subsequent invalid working ●⁴ is not available eg 282 → 360 – 282 = 078 Degree signs are not required Where an incorrect angle has been calculated ●⁴ can only be awarded where there is clear evidence of an intention to calculate angle T eg $\cos T = \frac{10 \cdot 3^2 + 7 \cdot 2^2 - 5 \cdot 6^2}{2 \times 10 \cdot 3 \times 7 \cdot 2}$ OR T = 31 OR angle marked at T on the diagram ●⁴ can only be awarded for adding 240 to a value previously calculated using trig. Disregard errors due to premature rounding provided there is evidence Inappropriate use of RAD or GRAD should only be penalised once in Q8, Q9, Q13 or Q17 (a) 240.73... (RAD) (b) 286.76... (GRAD) 			
<p>Commonly Observed Responses: Working must be shown.</p> <ol style="list-style-type: none"> <p>(a) $\cos T = \frac{10 \cdot 3^2 + 7 \cdot 2^2 - 5 \cdot 6^2}{2 \times 10 \cdot 3 \times 7 \cdot 2} = \frac{126.57}{148.32} \rightarrow 31 \rightarrow 271$ award 3/4 x✓✓✓ (see Note 4)</p> <p>(b) $\frac{10 \cdot 3^2 + 7 \cdot 2^2 - 5 \cdot 6^2}{2 \times 10 \cdot 3 \times 7 \cdot 2} = \frac{126.57}{148.32} \rightarrow 31 \rightarrow 271$ award 2/4 x✓✓x</p> <p>(a) $\cos T = \frac{7 \cdot 2^2 + 5 \cdot 6^2 - 10 \cdot 3^2}{2 \times 7 \cdot 2 \times 5 \cdot 6} = \frac{-22.89}{80.64} \rightarrow 106 \rightarrow 346$ award 3/4 x✓✓✓ (see Note 4)</p> <p>(b) $\frac{7 \cdot 2^2 + 5 \cdot 6^2 - 10 \cdot 3^2}{2 \times 7 \cdot 2 \times 5 \cdot 6} = \frac{-22.89}{80.64} \rightarrow 106 \rightarrow 346$ award 2/4 x✓✓x</p> 			

Question		Generic scheme	Illustrative scheme	Max mark
14.		<p>Method 1</p> <ul style="list-style-type: none"> •¹ isolate term in y or divide throughout by 5 •² state coordinates (must use brackets) <p>Method 2</p> <ul style="list-style-type: none"> •¹ substitute $x=0$ into equation •² state coordinates (must use brackets) 	<p>Method 1</p> <ul style="list-style-type: none"> •¹ $-5y = \dots + 20$ or $\dots - 20 = 5y$ or $\frac{2x}{5} - \frac{5y}{5} = \frac{20}{5}$ •² $(0, -4)$ <p>Method 2</p> <ul style="list-style-type: none"> •¹ $2 \times 0 - 5y = 20$ •² $(0, -4)$ 	2
<p>Notes:</p> <ol style="list-style-type: none"> 1. Correct answer without working award 2/2 2. Disregard errors in the x term for the award of •¹ 3. For finding where the line crosses the x-axis, $(10, 0)$, with working award 1/2 				
<p>Commonly Observed Responses</p> <ol style="list-style-type: none"> 1. $0, -4$ (no working necessary) award 1/2 ✓\times 2. $y = -4$ (no working necessary) award 1/2 ✓\times 				

Question		Generic scheme	Illustrative scheme	Max mark
15.		<ul style="list-style-type: none"> •¹ start to divide fractions •² factorise •³ multiply and simplify 	<ul style="list-style-type: none"> •¹ $\frac{n}{n^2-4} \times \frac{n-2}{3}$ •² $(n+2)(n-2)$ •³ $\frac{n}{3(n+2)}$ or $\frac{n}{3n+6}$ S 	3
<p>Notes:</p> <p>1. Correct answer without working 0/3</p> <p>2. For subsequent incorrect working, the final mark is not available</p> <p>eg (a) $\frac{n}{3(n+2)} = \frac{n}{3n+2}$ award 2/3 ✓✓x</p> <p>(b) $\frac{\cancel{n}}{3(\cancel{n}+2)} = \frac{1}{3(1+2)} = \frac{1}{9}$ award 2/3 ✓✓x</p>				
<p>Commonly Observed Responses:</p> <p>1. $\frac{n}{n^2-4} \div \frac{3(n+2)}{n^2-4} \rightarrow \frac{n}{n^2-4} \times \frac{n^2-4}{3(n+2)} \rightarrow \frac{n}{3(n+2)}$ award 3/3</p>				

Question		Generic scheme	Illustrative scheme	Max mark
16.		<ul style="list-style-type: none"> •¹ start valid strategy •² continue strategy •³ calculate length of space diagonal •⁴ valid conclusion with comparison 	<ul style="list-style-type: none"> •¹ $40^2 + 40^2$ or $40^2 + 70^2$ (stated or implied by •²) •² $\sqrt{40^2 + 40^2 + 70^2}$ •³ 90 •⁴ Yes, since $85 < 90$ 	4

Question	Generic scheme	Illustrative scheme	Max mark
<p>Notes:</p> <ol style="list-style-type: none"> Correct answer without working 0/4 Accept correct use of cosine rule Accept eg $\begin{pmatrix} -40 \\ 40 \\ 70 \end{pmatrix} \rightarrow \sqrt{(-40)^2 + 40^2 + 70^2}$ for the award of •¹ and •² •⁴ can only be awarded for a valid conclusion and comparison made with a value obtained from a Pythagoras (or trigonometric) calculation Award of •⁴: eg (a) $\sqrt{40^2 + 40^2 + 70^2} = 90$; Yes, since the umbrella is only 85 award 4/4 (b) $\sqrt{40^2 + 40^2 + 70^2} = 90$; Yes award 3/4 ✓✓✓x (c) $\sqrt{40^2 + 70^2} = 80 \cdot 62\dots$; No, since the locker is only 80·62... award 2/4 ✓xx✓ 			
<p>Commonly Observed Responses:</p> <ol style="list-style-type: none"> (a) $\sqrt{40^2 + 70^2} = 80 \cdot 62\dots$; No, since $85 > 80 \cdot 62\dots$ award 2/4 ✓xx✓ (b) $\sqrt{40^2 + 40^2} = 56 \cdot 56\dots$; No, since $85 > 56 \cdot 56\dots$ award 2/4 ✓xx✓ (a) $\sqrt{40^2 + 40^2} = 56 \cdot 56\dots = 57 \rightarrow \sqrt{57^2 + 70^2} = 90 \cdot 27 = 90$; Yes, since $85 < 90$ award 4/4 (b) $\sqrt{40^2 + 70^2} = 80 \cdot 62\dots = 81 \rightarrow \sqrt{81^2 + 40^2} = 90 \cdot 33 = 90$; Yes, since $85 < 90$ award 4/4 (a) $40^2 + 40^2 + 70^2 = 8100$; $85^2 = 7225$ Yes, since $8100 > 7225$ award 4/4 (b) $40^2 + 40^2 + 70^2 = 8100$; $85^2 = 7225$ Yes, since $8100 \neq 7225$ award 3/4 ✓✓✓x (a) $40^2 + 40^2 = 3200$; $85^2 = 7225$ No, since $3200 < 7225$ award 2/4 ✓xx✓ (b) $40^2 + 40^2 = 3200$; $85^2 = 7225$ No, since $3200 \neq 7225$ award 1/4 ✓xxx (c) $40^2 + 70^2 = 6500$; $85^2 = 7225$ No, since $6500 < 7225$ award 2/4 ✓xx✓ (d) $40^2 + 70^2 = 6500$; $85^2 = 7225$ No, since $6500 \neq 7225$ award 1/4 ✓xxx $40^2 + 40^2 = 3200$; $70^2 = 4900$ No, since $3200 < 4900$ award 1/4 ✓xxx 			

Question		Generic scheme	Illustrative scheme	Max mark
17.		<ul style="list-style-type: none"> •¹ substitute correctly into area of triangle formula •² appropriate fraction for sector •³ substitute correctly into area of sector formula •⁴ know to subtract area of sector from area of triangle •⁵ calculate area of shaded region and state correct units 	<ul style="list-style-type: none"> •¹ $\frac{1}{2} \times 38 \times 55 \times \sin 75 (= 1009.39\dots)$ •² $\frac{75}{360}$ •³ $\frac{75}{360} \times \pi \times 30^2 (= 589.04\dots)$ •⁴ evidence of area of triangle – area of sector •⁵ $420(.3\dots) \text{ cm}^2$ 	5

Question	Generic scheme	Illustrative scheme	Max mark
<p>Notes:</p> <ol style="list-style-type: none"> Correct answer without working award 0/5 Accept variations in π Disregard errors due to premature rounding provided there is evidence Inappropriate use of GRAD leading to $376(.40\dots)$ cm² should only be penalised once in Q8, Q9, Q13 or Q17 The following answers should be awarded <ul style="list-style-type: none"> 4/5 if the use of RAD has already been penalised in Q8, Q9 or Q13 3/5 if the use of RAD has not already been penalised in Q8, Q9 or Q13 <ol style="list-style-type: none"> $-405(.23\dots) - 589(.04) = -994(.28\dots)$ cm² $405(.23\dots) - 589(.04) = -183(.81\dots)$ cm² $589(.04) - 405(.23\dots) = 183(.81\dots)$ cm² $589(.04) - (-405(.23\dots)) = 994(.28\dots)$ cm² ⁵ is only available for calculating the sum or difference of the area of a triangle and the area of a sector, where the area of the triangle is calculated using trigonometry 			
<p>Commonly Observed Responses: Working must be shown:</p> <ol style="list-style-type: none"> $\frac{1}{2} \times 38 \times 55 \times \sin 75 - \frac{75}{360} \times \pi \times 60 = 970(.1\dots)$ cm² award 4/5 ✓✓x✓✓ $\frac{1}{2} \times 38 \times 55 \times \sin 75 + \frac{75}{360} \times \pi \times 30^2 = 1598(.4\dots)$ cm² award 4/5 ✓✓✓x✓ $\frac{1}{2} \times 38 \times 55 \times \sin 75 + \frac{75}{360} \times \pi \times 60 = 1048(.6\dots)$ cm² award 3/5 ✓✓xx✓ $\frac{75}{360} \times \pi \times 30^2 = 589(.0\dots)$ cm² award 2/5 x✓✓xx $\frac{1}{2} \times 38 \times 55 \times \sin 75 = 1009(.3\dots)$ cm² award 1/5 ✓xxxx $\pi \times 30^2 = 2827(.4\dots)$ cm² award 0/5 			

Question		Generic scheme	Illustrative scheme	Max mark
18.	(a)	<p><u>Method 1</u></p> <ul style="list-style-type: none"> •¹ state linear scale factor •² know to multiply volume by cube of linear scale factor •³ correct calculation (must involve a power of the scale factor), valid comparison and conclusion <p><u>Method 2</u></p> <ul style="list-style-type: none"> •¹ state linear scale factor •² know to divide volume by cube of linear scale factor •³ correct calculation (must involve a power of the scale factor), valid comparison and conclusion <p><u>Method 3</u></p> <ul style="list-style-type: none"> •¹ state volume scale factor •² know to multiply depth by cube root of volume scale factor •³ correct calculation (must involve a root of the volume scale factor), valid comparison and conclusion <p><u>Method 4</u></p> <ul style="list-style-type: none"> •¹ state linear scale factor •² know to compare cube of linear scale factor with volume scale factor •³ correct calculation (must involve a power of the scale factor), valid comparison and conclusion 	<p><u>Method 1</u></p> <ul style="list-style-type: none"> •¹ eg $\frac{24}{16}$ or equivalent •² $576 \times \left(\frac{24}{16}\right)^3$ •³ $1944 \neq 1125$, so the cartons are not similar <p><u>Method 2</u></p> <ul style="list-style-type: none"> •¹ eg $\frac{16}{24}$ or equivalent •² $576 \div \left(\frac{16}{24}\right)^3$ •³ $1944 \neq 1125$, so the cartons are not similar <p><u>Method 3</u></p> <ul style="list-style-type: none"> •¹ eg $\frac{1125}{576}$ or equivalent •² $\sqrt[3]{\frac{1125}{576}} \times 16$ •³ $20 \neq 24$, so the cartons are not similar <p><u>Method 4</u></p> <ul style="list-style-type: none"> •¹ eg $\frac{24}{16}$ or equivalent •² $\left(\frac{24}{16}\right)^3$ and $\frac{1125}{576}$ •³ $3.375 \neq 1.95\dots$, so the cartons are not similar 	3

Question		Generic scheme	Illustrative scheme	Max mark
18.	(a)	<p>Method 5</p> <ul style="list-style-type: none"> •¹ state volume scale factor •² know to compare cube root of volume scale factor with linear scale factor •³ correct calculation (must involve a root of the volume scale factor), valid comparison and conclusion 	<p>Method 5</p> <ul style="list-style-type: none"> •¹ eg $\frac{1125}{576}$ or equivalent •² $\sqrt[3]{\frac{1125}{576}}$ and $\frac{24}{16}$ •³ $1.25 \neq 1.5$, so the cartons are not similar 	

Notes:

1. Correct answer without working award 0/3
2. For the award of •¹ accept a rounded or truncated decimal equivalent (to at least 2 decimal places) for evidence of the scale factor eg $\frac{1125}{576} = 1.95$, $\frac{16}{24} = 0.66$; but see Note 3
3. Where premature rounding leads to an inaccurate answer, •³ is not available
eg $1125 \times \left(\frac{16}{24}\right)^3 \rightarrow 1125 \times 0.7^3 = 385.875$; $385.875 \neq 576$, so the cartons are not similar
award 2/3 ✓✓x
4. For the award of •³ there must be a numerical comparison or a statement such as ‘the two scale factors are different’; a simple statement of ‘not similar’ is not sufficient

Commonly Observed Responses:

1. $1125 \times \left(\frac{16}{24}\right)^3 = 333.3\dots$; $333.3 \neq 576$, so the cartons are not similar award 3/3
2. (a) $576 \times \frac{24}{16} = 864$; $864 \neq 1125$, so the cartons are not similar award 1/3 ✓xx
(b) $576 \times \frac{16}{24} = 384$; $384 \neq 1125$, so the cartons are not similar award 1/3 ✓xx
3. (a) $576 \times \left(\frac{24}{16}\right)^2 = 1296$; $1296 \neq 1125$, so the cartons are not similar award 2/3 ✓x✓
(b) $576 \times \left(\frac{16}{24}\right)^2 = 256$; $256 \neq 1125$, so the cartons are not similar award 2/3 ✓x✓
4. (a) $\frac{576}{16^3} = 0.14\dots$, $\frac{1125}{24^3} = 0.08\dots$; $0.14\dots \neq 0.08\dots$, so the cartons are not similar award 3/3
(b) $\frac{576}{16^2} = 2.25$, $\frac{1125}{24^2} = 1.95\dots$; $2.25 \neq 1.95\dots$, so the cartons are not similar award 2/3 ✓x✓
(c) $\frac{576}{16} = 36$, $\frac{1125}{24} = 46.875$; $36 \neq 46.875$, so the cartons are not similar award 1/3 ✓xx

Question		Generic scheme	Illustrative scheme	Max mark
18.	(b)	<p>Method 1</p> <ul style="list-style-type: none"> •¹ find volume scale factor •² correct calculation to find height (must involve a root of the volume scale factor) <p>Method 2</p> <ul style="list-style-type: none"> •¹ find volume scale factor •² correct calculation to find height (must involve a root of the volume scale factor) 	<p>Method 1</p> <ul style="list-style-type: none"> •¹ $\frac{1500}{576}$ •² $\sqrt[3]{\frac{1500}{576}} \times 16 = 22(\cdot 0\dots \text{ cm})$ <p>Method 2</p> <ul style="list-style-type: none"> •¹ $\frac{576}{1500}$ •² $16 \div \sqrt[3]{\frac{576}{1500}} = 22(\cdot 0\dots \text{ cm})$ 	2

Notes:

1. Correct answer without working award 0/2
2. Disregard errors due to premature rounding provided there is evidence

Commonly Observed Responses:

1. $\frac{1500}{576} \times 16 = 41.66\dots$ award 1/2 ✓ x
2. $\sqrt{\frac{1500}{576}} \times 16 = 25.81\dots$ award 1/2 ✓ x
3. $\sqrt[3]{\frac{1500}{1125}} \times 24 = 26.41\dots$ award 1/2 x ✓

[END OF MARKING INSTRUCTIONS]